

Answer on Question #56125 – Math – Vector Calculus

Let $\varphi = 2xz^4 - x^2y$, find

$$|\nabla\varphi|$$

$$5(\sqrt{97})$$

$$3(\sqrt{112})$$

$$(\sqrt{105})$$

$$2(\sqrt{93})$$

Solution

$$\nabla\varphi = \left(\frac{\partial\varphi}{\partial x}, \frac{\partial\varphi}{\partial y}, \frac{\partial\varphi}{\partial z} \right) = \left(\frac{\partial(2xz^4 - x^2y)}{\partial x}, \frac{\partial(2xz^4 - x^2y)}{\partial y}, \frac{\partial(2xz^4 - x^2y)}{\partial z} \right) = (2z^4 - 2xy, -x^2, 8xz^3).$$

$$|\nabla\varphi| = \sqrt{(2z^4 - 2xy)^2 + (-x^2)^2 + (8xz^3)^2}.$$

If we need the number in the answer we need to choose a point (x_0, y_0, z_0) where we calculate $|\nabla\varphi|$.