limit $\Delta x$ tends to $0 ; \Delta y / \Delta x=d y / d x$. why we use $\Delta x$ tends to 0 here ?? what does it mean?

## Solution

The slope $m$ of the secant line is the difference between the $y$ values of these points divided by the difference between the $x$ values, that is,
$m=\frac{\Delta y(x)}{\Delta x}$
The limit of the secant lines is the tangent line. Therefore, the limit of the difference quotient as $\Delta x$ approaches zero, if it exists, should represent the slope of the tangent line. This limit is defined to be the derivative of the function $y(x)$ :

$$
y^{\prime}(x)=\lim _{\Delta x-0} \frac{y(x+\Delta x)-y(x)}{\Delta x} .
$$

