

Answer on Question #51467 – Math – Statistics and Probability

If a random variable X has a cumulative distribution function $F(x)$ given by

$$0, x \leq 0$$

$$F(x) = c(x - e^{-x}), 0 < x < 1$$

$$1, x \geq 1$$

then find its corresponding probability distribution function and hence calculate

$$P(0 < x < 1)$$

Solution.

There was a mistake in assignment, because $F(x)$ is related to probability, but probability is not greater than 1.

A cumulative distribution function of X is given by

$$F(x) = \begin{cases} 0, & x \leq 0 \\ c(x - e^{-x}), & 0 < x < 1 \\ 1, & x \geq 1 \end{cases}$$

$$\text{Probability distribution function } p(x) = \frac{dF}{dx} = \begin{cases} 0, & x \leq 0 \\ c(1 + e^{-x}), & 0 < x < 1 \\ 0, & x \geq 1 \end{cases}$$

$$P(0 < X < 1) = P(X < 1) - P(X \leq 0) = F(1) - \lim_{x \rightarrow 0^+} F(x) = 1 - c.$$