Answer on Question #47799 - Math - Geometry

I have a simple right angle triangle. All I am given is h (the hypotenuse) and that ratio of x:y is 2:3. What is the formula to find x and y in terms of h?

Solution

$$\frac{x}{y} = \frac{2}{3} \implies 3x = 2y \implies y = \frac{3}{2}x$$

Write the Pythagorean theorem:

$$x^{2} + \left(\frac{3}{2}x\right)^{2} = h^{2}$$

$$\frac{13}{4}x^{2} = h^{2}$$

$$\frac{\sqrt{13}}{2}x = h$$

$$x = \frac{2h}{\sqrt{13}}$$

$$y = \frac{3}{2}x = \frac{3}{\sqrt{13}}h$$

Answer:

$$x = \frac{2h}{\sqrt{13}}$$
$$y = \frac{3}{\sqrt{13}}h$$