

Answer to Question #46133 – Math – Integral Calculus

Find the $\int \tan^3 x \sec^3 x dx$

- tan²x+1
- cot²x+1
- sec²x+1
- sec²x

Solution:

$$\begin{aligned}\int \tan^3 x * \sec^3 x dx &= \int \frac{\sin^3 x}{\cos^3 x} * \frac{1}{\cos^3 x} dx = \\&= - \int \frac{\sin^2 x}{\cos^6 x} d \cos x = \int \frac{\cos^2 x - 1}{\cos^6 x} d \cos x = \int \left(\frac{1}{\cos^4 x} - \frac{1}{\cos^6 x} \right) d \cos x = \\&= \frac{1}{5 * \cos^5 x} - \frac{1}{3 * \cos^3 x} + C\end{aligned}$$

where C is an arbitrary constant.

Answer:

$$\int \tan^3 x * \sec^3 x dx = \frac{1}{5 * \cos^5 x} - \frac{1}{3 * \cos^3 x} + C$$

P. S.: maybe you make some mistake in task $\int \tan^3 x \sec^3 x dx$.