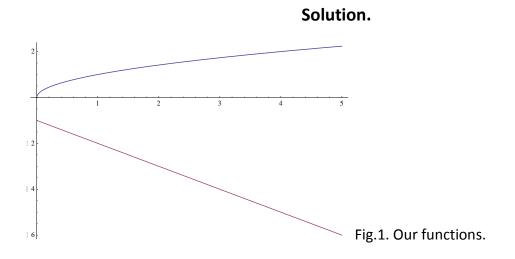
Question.

Find the area of the region bounded by the graphs of \sqrt{x} and y = -x - 1 between x = 1 and x = 4.

19/6

1/4

14π/5 1/2



As we know, the area under the non-negative function is defined as integral of non-negative function. But in our case, we must calculate the sum of two integrals with two functions. Because the integral gives only the area between the curve and the x-axes.

Function \sqrt{x} is non-negative for $1 \le x \le 4$, function (-x - 1) is negative for $1 \le x \le 4$. To evaluate the area bounded by the graph of y = -x - 1 and x-axis between x = 1 and x = 4, we take expression (-x - 1) with the opposite sign in the definite integral.

So, let calculate the area between the functions:

$$A = \int_{1}^{4} \sqrt{x} \, dx - \int_{1}^{4} (-x - 1) \, dx = \frac{2}{3} x^{\frac{3}{2}} \Big|_{1}^{4} + \int_{1}^{4} (x + 1) \, dx = \frac{2}{3} (8 - 1) + \left(\frac{x^{2}}{2} + x\right) \Big|_{1}^{4} = \frac{14}{3} + (8 + 4 - \frac{1}{2} - 1) = \frac{14}{3} + \frac{21}{2} = \frac{28 + 63}{6} = \frac{91}{6}$$

Answer.

 $A = \frac{91}{6}$, correct answers were absent.

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