

Answer on Question #45785 - Math - Calculus

$$f(x) = 3x + 5,$$

$$g(x) = 6x^2$$

Find $(fg)(x)$.

Solution

Consider F to be domain of the function $f(x)$, G to be domain of the function $g(x)$, H to be domain of the expression $(fg)(x)$.

$(fg)(x) = f(x)g(x)$. Domain of the whole expression is nothing else but intersection of the function's domains: $H = F \cap G$.

Particular case of the task:

$$f(x) = 3x + 5. \text{ It's domain: } F = \mathbb{R}.$$

$$g(x) = 6x^2. \text{ It's domain: } G = \mathbb{R}.$$

Thus,

$$(fg)(x) = f(x)g(x) = (3x + 5)(6x^2) = 3x \times 6x^2 + 5 \times 6x^2 = 18x^3 + 30x^2,$$

$$H = F \cap G = \mathbb{R} \cap \mathbb{R} = \mathbb{R}.$$

Answer: $(fg)(x) = 18x^3 + 30x^2$.