Answer on Question #44923 – Math - Linear Algebra

If zero is an eigenvalue of a linear transformation T, then T is not invertible.

Answer

True. If zero is an eigenvalue of a linear transformation T, so there is at least one non-zero vector \vec{v} such that $T\vec{v} = 0$ (0 is an eigenvalue of T with corresponding eigenvector \vec{v}). We see that the nullspace of T has dimension ≥ 1 . Since

$$\dim \operatorname{col} T + \dim \operatorname{nul} T = n$$

and

 $\dim col T = rank T$

rank T < n. Then T is not invertible.