

Answer on Question #44663 – Math – Geometry

Question

The silo on a farm is a composite figure. What two shapes make up the silo? Choose an answer from below.

- A. Prism and Sphere
- B. Prism and Hemisphere
- C. Cylinder and Sphere
- D. Cylinder and Hemisphere

To the nearest pound, how much grain with the silo hold if the height of the ladder is 40 feet and the radius is 6 feet? (1 cubic foot = 62.43 pounds)

Answer

The correct answer is **D. Cylinder and Hemisphere**.

Given

$R = 6$ feet – radius of the silo

$H = 40$ feet – height of the ladder

$d = 62.43$ pounds/cubic foot – packed density of the grain

Solution

Total volume of the silo is equal to the sum of volumes of its cylindrical part and its hemispherical part:

$$V_{\text{sil}o} = V_c + V_{hs}$$

Volume of the cylindrical part of the silo:

$$V_c = \pi R^2 H = 3.14 \cdot (6 \text{ feet})^2 \cdot 40 \text{ feet} = 4522 \text{ cubic feet}$$

Volume of the hemispherical part of the silo:

$$V_{hs} = \frac{2}{3} \pi R^3 = \frac{2}{3} 3.14 \cdot (6 \text{ feet})^3 = 452 \text{ cubic feet}$$

Total volume of the silo:

$$V_{\text{sil}o} = 4522 + 452 = 4974 \text{ cubic feet}$$

Mass of the grain hold in the silo:

$$m = V_{\text{sil}o} \cdot d = 4974 \text{ cubic feet} \cdot 62.43 \frac{\text{pounds}}{\text{cubic foot}} = 310526.82 \text{ pounds}$$

Answer: 310526.82 pounds