

Answer on Question #44533 – Math - Algebra

Task:

Consider the sets $A = \{3x | x \in \mathbb{Z}\}$, $B = \{x \in \mathbb{Q} | -5 \leq x \leq 10\}$, $C = \{\text{factors of 20 in } \mathbb{Z}\}$.

Represent $A \cap B$, $BC \cup C$ and $C \setminus A$ by the listing method and in a single Venn diagram.

Solution:

$A \cap B$:

$$A = \{0, 3, -3, 6, -6, 9, -9, 12, -12, \dots\};$$

$$B = \{x \in \mathbb{Q} | -5 \leq x \leq 10\} = \{-5, \dots, -3, \dots, 0, \dots, 1, \dots, 3, \dots, 6, \dots, 9, \dots, 10\}; \text{ So, } A \cap B = \{-3, 0, 3, 6, 9\};$$

$BC \cup C$:

$$B = \{x \in \mathbb{Q} | -5 \leq x \leq 10\}; C = \{1, -1, 2, -2, 4, -4, 5, -5, 10, -10, 20, -20\};$$

$$BC = \{-5, -4, -2, -1, 1, 2, 4, 5, 10\}; \text{ So } BC \cup C = \{-1, 1, 2, -2, 4, -4, 5, -5, 10, -10, 20, -20\};$$

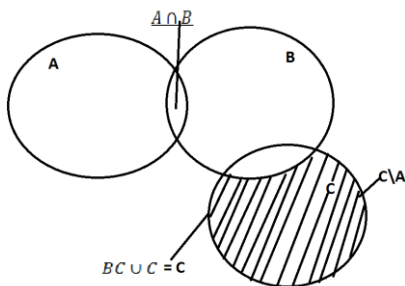
$C \setminus A$:

$$C = \{1, -1, 2, -2, 4, -4, 5, -5, 10, -10, 20, -20\};$$

$$A = \{0, 3, -3, 6, -6, 9, -9, 12, -12, 15, -15, 18, -18, 21, -21, \dots\};$$

$$C \setminus A = \{1, -1, 2, -2, 4, -4, 5, -5, 10, -10, 20, -20\};$$

Venn diagram:



Answer:

$$\text{So, } A \cap B = \{-3, 0, 3, 6, 9\}$$

$$BC \cup C = \{-1, 1, 2, -2, 4, -4, 5, -5, 10, -10, 20, -20\}$$

$$C \setminus A = \{1, -1, 2, -2, 4, -4, 5, -5, 10, -10, 20, -20\}$$