Answer on Question #44413 – Math - Algebra

1. A largest possible cylinder will be removed from a cube of edge (4x) cm. Express the volume of the remaining solid as product of two polynomials.

2. The radius of th circular base of a cone is (3x - 2) meters. If its slant height is $(9x^2 - 6x)$ meters, express the cone's surface area as a product of polynomials in x.

Solution:



Edge of cube is equal 4x cm. The volume of the remaining solid (cube without cylinder) is equal to volume of cube subtract volume of cylinder.

For a cube of edge with length a, volume is equal to a³. For **right circular cylinder**, i.e., the cylinder with the generating lines perpendicular to the bases, with its ends closed to form two circular surfaces, as in the figure, we have, If the cylinder has a <u>radius</u> r and length (height) h, then its <u>volume</u> is given by

 $V = \pi r^2 h.$

For our **cylinder** we have $r=\frac{4x}{2}=2x$ (half edges of a cube) and h=4x (equal edges of a cube). Hence $V_{cube} = (4x)^3 = 64x^3 (cm^3)$ and $V_{cylinder} = \pi (2x)^2 4x = 16\pi x^3 (cm^3)$. Therefore volume of the remaining solid $V_{rem,solid}=64x^3 - 16\pi x^3 = 16x^3(4-\pi)$ (cm³)

Answer: $V_{rem.solid}=16x^3(4-\pi)$ (cm³)(it is product of two polynomial of x: thihrd and nill degrees)

2. We have drawing:



The lateral surface area of a right circular cone is $LSA = \pi rl$ where r is the radius of the circle at the bottom of the cone and l is the slant height of the cone (given by the Pythagorean theorem

 $l = \sqrt{h^2 + r^2}$ where *h* is the height of the cone). The surface area of the bottom circle of a cone is the same as for any circle, πr^2 . Thus the total surface area of a right circular cone is:

$$SA = \pi r^{2} + \pi r l = \pi r (r + l).$$

We have $r = 3x - 2$ and $l = 9x^{2} - 6x$. Hence h=
 $\sqrt{(9x^{2} - 6x)^{2} - (3x - 2)^{2}} = \sqrt{81x^{4} - 108x^{3} + 27x^{2} + 12x - 4}.$
Therefore **answer**
 $SA = \pi r (r + l) = \pi (3x - 2)(3x - 2 + \sqrt{81x^{4} - 108x^{3} + 27x^{2} + 12x - 4}).$

P. S.:

I assume in the task mistake, because

 $\pi(3x-2)(3x-2+\sqrt{81x^4-108x^3+27x^2+12x-4})$

is not a product of polynomials in x.

Maybe in the task was meant to find lateral surface area of cone $LSA = \pi rl$. If that true, then

 $LSA = \pi(3x-2)(9x^2-6x) = 3\pi x(9x^2-12x+4)$ is a product of polynomials in x.

Remark: when writing "cone's surface area" in most cases it's mean, total surface area.