

Answer on Question #43729 – Math – Trigonometry

prove that $\sin^3 a + \cos^3 a / \sin a + \cos a = 1 - \frac{1}{2} \sin 2a$

Answer.

$$\begin{aligned} \frac{\sin^3 \alpha + \cos^3 \alpha}{\sin \alpha + \cos \alpha} &= \frac{(\sin \alpha + \cos \alpha)(\sin^2 \alpha - \sin \alpha \cos \alpha + \cos^2 \alpha)}{\sin \alpha + \cos \alpha} = 1 - \sin \alpha \cos \alpha = \\ &= 1 - \frac{1}{2} \sin 2\alpha. \quad \text{Q.E.D.} \end{aligned}$$