

Answer on Question#43683 – Math – Abstract Algebra

Question:

Solve the following system of equations, state the method that you would use, and show all work to solve:

$$5x - 3y = -4$$

$$3x - y = -4$$

$$x + 5y = 12$$

$$5x + 25y = 12$$

$$x + y = -2$$

$$-3x - 3y = 6$$

Solution.

To solve the first system we will use the substitution method.

From second equation we have: $y=3x+4$. Substituting it in the first equation we get :

$$5x - 3(3x+4) = -4$$

$$5x - 9x - 12 = -4$$

$$-4x = 8$$

$$x = -2.$$

And coming back to the first equation we get:

$y=3(-2)+4=-2$. So, the solution is $x=-2, y=-2$.

Answer. $x = -2, y = -2$.

To solve the second equation let's use the substitution method again.

From first equation we have: $x=12-5y$. Substituting it in the second equation we get

$$5(12-5y)+25y=12$$

$$60-25y+25y=12$$

$$\text{we get } 60=12$$

so, we see that this system has no solution.

Answer. No solution.

And to solve the last equation we will use the addition method.

Firstly let's divide the second equation by -3, we get : $x+y=-2$. Hence, the system is consisting from 2 identical equations. Hence, we get the whole line of solutions $y=-2-x$.

Answer. The solutions are all points which satisfies $y = -2 - x$.