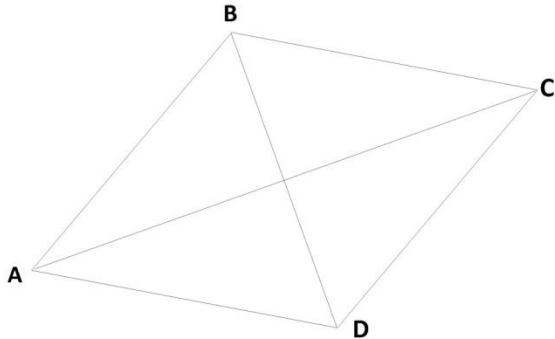


Answer on Question #43545, Math, Other

Task: Prove that in any parallelogram the sum of the squares on the diagonals is twice the sum of the squares on two adjacent sides.

Answer:



We have parallelogram ABCD with diagonals AC and BD. Using the Law of Cosines:

$$\triangle ABC : AC^2 = AB^2 + BC^2 - 2 \cdot AB \cdot BC \cdot \cos \angle B;$$

$$\text{In } \triangle ABD : BD^2 = AB^2 + AD^2 - 2 \cdot AB \cdot AD \cdot \cos \angle A;$$

But $AD = BC$; $\angle A = 180^\circ - \angle B$.

$$BD^2 = AB^2 + BC^2 - 2 \cdot AB \cdot BC \cdot \cos(180^\circ - \angle B) \Rightarrow$$

So we have $BD^2 = AB^2 + BC^2 + 2 \cdot AB \cdot BC \cdot \cos \angle B$; \Rightarrow

$$AC^2 + BD^2 = 2(AB^2 + BC^2)$$