

Answer on Question #42777 – Math - Calculus

Using the given zero, find one other zero of $f(x)$. Explain the process you used to find your solution.

$2 - 3i$ is a zero of $f(x) = x^4 - 4x^3 + 14x^2 - 4x + 13$.

Solution:

We will use Horner's method (http://en.wikipedia.org/wiki/Horner%27s_method).

So we will create a table of coefficients of equation $x^4 - 4x^3 + 14x^2 - 4x + 13 = 0$:

| | | | | | |
|--|----------|-----------|-----------|-----------|-----------|
| | 1 | -4 | 14 | -4 | 13 |
| | | | | | |
| | | | | | |

We will try $(2 + 3i)$ as a zero of the equation:

| | | | | | |
|---------------|----------|-----------|-----------|-----------|-----------|
| | 1 | -4 | 14 | -4 | 13 |
| | | | | | |
| 2 + 3i | | | | | |

We copy a first coefficient and put it below:

| | | | | | |
|---------------|----------|-----------|-----------|-----------|-----------|
| | 1 | -4 | 14 | -4 | 13 |
| | | | | | |
| 2 + 3i | 1 | | | | |

Then we multiply my new zero $(2+3i)$ and "1" and put answer in the table:

| | | | | | |
|---------------|----------|-------------|-----------|-----------|-----------|
| | 1 | -4 | 14 | -4 | 13 |
| | | 2+3i | | | |
| 2 + 3i | 1 | | | | |

Then we add “-4” and $(2+3i)$ and put answer in the table:

| | | | | | |
|----------|---|---------------------------|----|----|----|
| | 1 | -4 | 14 | -4 | 13 |
| | | $2+3i$ | | | |
| $2 + 3i$ | 1 | $-2+3i$ | | | |

Then we multiply $(2 + 3i)(-2 + 3i) = -4 - 6i + 6i + 9i^2 = -4 - 9 = -13$ and put it in the table.

| | | | | | |
|----------|---|---------|------------|----|----|
| | 1 | -4 | 14 | -4 | 13 |
| | | $2+3i$ | -13 | | |
| $2 + 3i$ | 1 | $-2+3i$ | | | |

Analogically till the end of the table:

| | | | | | |
|----------|---|---------|-----|---------|-----|
| | 1 | -4 | 14 | -4 | 13 |
| | | $2+3i$ | -13 | $2+3i$ | -13 |
| $2 + 3i$ | 1 | $-2+3i$ | 1 | $-2+3i$ | 0 |

We have received zero in the end. It means, that $(2+3i)$ is a zero of the equation.

Answer:

$2+3i$