Answer on Question #42774 – Math – Calculus

State how many imaginary and real zeros the function has.

 $f(x) = x^3 + 5x^2 + x + 5$

Solution.

$$x^{3} + 5x^{2} + x + 5 = 0$$
$$x(x^{2} + 1) + 5(x^{2} + 1) = 0$$
$$x(x^{2} + 1) + 5(x^{2} + 1) = 0$$
$$(x^{2} + 1)(x + 5) = 0$$

So we get $x^2 + 1 = 0$ or x + 5 = 0. Hence, the zeros of f(x) are $x_1 = i$, $x_2 = -i$, $x_3 = -5$

Answer. 1 real zero x=-5, and two imaginary zeros x=I and x=-i.