Answer on Question #42448, Math, Geometry

Problem.

State whether the given measurements determine zero, one, or two triangles.

$$C = 30^{\circ}$$
, $a = 32$, $c = 16$

Help me please

Solution.

The Law of Sines gives $\frac{\sin A}{a} = \frac{\sin C}{c} \Rightarrow \sin A = \sin C \frac{a}{c} = 0.5 \frac{32}{16} = 1 \Rightarrow A = 90^{\circ}$. So, the triangle is right and $B = 90^{\circ} - C = 60^{\circ}$.

Then, from the Pythagorean theorem, $b=\sqrt{a^2-c^2}=\sqrt{32^2-16^2}=16\sqrt{3}\approx 27.7128$. So, the answer is: one triangle.