

Answer on Question #42249-Math-Statistics and Probability

Assume that the samples are independent and that they have been randomly selected. Construct a 90% confidence interval for the difference between population proportions $p_1 - p_2$. Round to three decimal places.

$$x_1=24, n_1=51, x_2=29, n_2=56$$

Solution

The confidence interval estimate of the difference $p_1 - p_2$ is

$$\widehat{p}_1 - \widehat{p}_2 - E < p_1 - p_2 < \widehat{p}_1 - \widehat{p}_2 + E.$$

Where the margin of error E is given by

$$E = z_{\alpha/2} \sqrt{\frac{\widehat{p}_1 \cdot \widehat{q}_1}{n_1} + \frac{\widehat{p}_2 \cdot \widehat{q}_2}{n_2}}.$$

$$x_1 = 24, n_1 = 51, x_2 = 29, n_2 = 56.$$

$$\widehat{p}_1 - \widehat{p}_2 = \frac{x_1}{n_1} - \frac{x_2}{n_2} = \frac{24}{51} - \frac{29}{56} = -0.047.$$

$z_{\alpha/2}$ for a 90% confidence interval is $z_{0.05} = 1.645$.

$$E = 1.645 \cdot \sqrt{\frac{24 \cdot 27}{51 \cdot 51} + \frac{29 \cdot 27}{56 \cdot 56}} = 0.159.$$

The confidence interval estimate of the difference $p_1 - p_2$ is

$$-0.047 - 0.159 < p_1 - p_2 < -0.047 + 0.159.$$

Answer: (-0.206; 0.112).