Answer on Question # 42002 – Math – Calculus

The intensity I of light varies inversely as the square of the distance D from the source. If the intensity of illumination on a screen 5 ft from a light is 4 foot candles, find the intensity on a screen 20 ft from the light.

Solution:

Intensity varies iversely as the square of the distance D from the source (k - coefficient):

$$I = \frac{k}{D^2}$$

In first case ($D_1 = 5$ ft, $I_1 = 4$ fc):

$$I_1 = \frac{k}{D_1^2}$$
 (1)

In second case ($D_2 = 20$ ft)::

$$I_{2} = \frac{k}{D_{2}^{2}} \quad (2)$$

$$(2) \div (1):$$

$$\frac{I_{2}}{I_{1}} = \frac{k}{D_{2}^{2}} \cdot \frac{D_{1}^{2}}{k} = \frac{D_{1}^{2}}{D_{2}^{2}}$$

$$I_{2} = I_{1} \frac{D_{1}^{2}}{D_{2}^{2}} = 4fc \cdot \frac{(5 \text{ ft})^{2}}{(20 \text{ ft})^{2}} = 0.25fc$$

Answer: intensity is equal to 0.25 foot candles.