

Answer on Question #40381, Math, Linear Algebra

If  $\mathbf{V}$  is an eigenvector of an  $n \times n$  invertible matrix  $A$ , then  $\mathbf{V}$  is also an eigenvector of the matrix  $A^2$ .

**Solution.**

Suppose

$$A\mathbf{V} = \lambda\mathbf{V}$$

Then we have

$$A^2\mathbf{V} = A(A\mathbf{V}) = A(\lambda\mathbf{V}) = \lambda A\mathbf{V} = \lambda^2\mathbf{V}.$$

**Answer:**

So  $\mathbf{V}$  is an eigenvector of  $A^2$  with eigenvalue  $\lambda^2$ .