

Answer on Question #38962-Math-Math, Other

- 1) Let's prove that **L1** is not regular. We can use pumping lemma. If **L1** is regular, there exist such **n** that we can pump any balanced parenthesis longer than **n**. OK. Then we can do this
 $n n$
to this one: (). Obviously, after pumping new parenthesis is unbalanced.
- 2) Let's prove that **L2** is not regular. We can use pumping lemma again. There is no infinite sequence of Fibonacci numbers with constant difference between neighboring elements.
- 3) Let's prove that **L3** is regular. Any Fibonacci number larger than 5 can be represented as $13x + 8y$. And any number from closure under addition of Fibonacci numbers larger than 5 can be too. Then we can use this prefix grammar:
 $\Sigma: \{a\}$.
 $S: \{\epsilon\}$.
P:
 $\epsilon \rightarrow aaaaaaaa;$
 $\epsilon \rightarrow aaaaaaaaaaaaaa.$

Proved!

Answer: C.