

## Question#38671, Math, Calculus

Find the limit if it exist. If it does not exist explain why.

Two questions

1

Limit of  $\cot x$

As  $x$  approaches  $\pi$

and

2

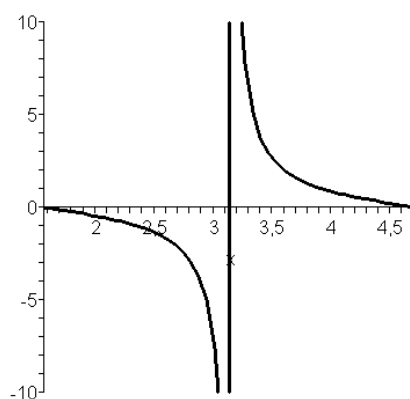
Limit of  $(2 - \text{absolute}(-x))$

As  $x$  approaches 3

I have the answers from the book but dont understand what process I need to get there. #1 doesnt exist but my in my calc it looks like its 18.something. #2 I substituted in the 3 but get -1 but it also doesnt exist somehow.

### Solution

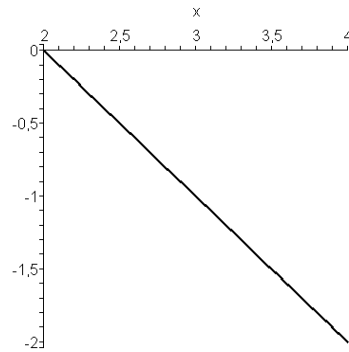
1. We start from an informal definition. The function  $f(x)$  is said to have the limit  $l$  as  $x$  approaches (or tends to)  $a$  if the values of  $f(x)$  can be made as close as we like to  $l$  by taking  $x$  sufficiently close to  $a$ . If we scetch the  $\cot x$  graph on the segment  $[\pi/2, 3\pi/2]$  we must conclude that this function has no limit as  $x$  approaches  $\pi$  in the sense of previous definition, because the graph has a vertical asymptote when  $x = \pi/2$ .



The function  $\cot x$  values cannot group around any number near the point  $x = \pi$ , but if  $x$  tends to  $\pi$  then  $\cos x$  tends to 1 ( $\cos x \approx 1$ ), and  $\sin x$  tends to 0, so the fraction  $\cos x/\sin x =$  tends to infinity and we can write

$$\lim_{x \rightarrow \pi} \cot x = \infty.$$

2. It is also useful to sketch the function graph on the segment  $[2, 4]$ .



From this graph one can see that the function  $2 - |x|$  approaches  $-1$  as  $x$  approaches  $3$ . It is easy to explain. We have  $|-x| = |x|$ , if  $x \geq 2$ , then  $|x| = x$ , and by using the well known limit theorems we obtain

$$\lim_{x \rightarrow 3} (2 - |-x|) = \lim_{x \rightarrow 3} (2 - x) = \lim_{x \rightarrow 3} 2 - \lim_{x \rightarrow 3} x = 2 - 3 = -1.$$