

**Answer on Question#38332 - Math - Calculus**

Find the function's domain and range. Next, describe level curves of the functions

a)  $f(x,y)=x-y$

b)  $f(x,y)=x^2+y^2$

c)  $f(x,y,z)=x+y+z$

**Solution**

a)  $f(x,y)=x-y$

The domain is all the values that go into a function. Both  $x$  and  $y$  can be values from  $-\infty$  to  $+\infty$  (this is the domain)

The range is all the values that are produced by the function, i.e. the values of  $f(x,y)$  in this example can range from  $-\infty$  to  $+\infty$

Direct Line - graph of a linear function  $y = x$ . This straight line passes through the origin. As the domain and range are all the values from  $-\infty$  to  $+\infty$  that the graph of function is all points in the plane.

b)  $f(x,y)=x^2+y^2$

The domain is all the values that go into a function. Both  $x$  and  $y$  can be values from  $-\infty$  to  $+\infty$  (this is the domain)

The range is all non-negative real numbers,  $\{f \in \mathbb{R} : f \geq 0\}$

The graph of function  $x^2+y^2 = r^2$  is a circle centered at the origin. As the domain is the values from  $-\infty$  to  $+\infty$  that the graph of function is all points in the plane.

c)  $f(x,y,z)=x+y+z$

The domain is all the values that go into a function. All  $x,y$  and  $z$  can be values from  $-\infty$  to  $+\infty$  (this is the domain)

The range is all real numbers.

Graph of this function is the whole plane in three-dimensional space.