

## Answer on Question #37888 – Math - Statistics and Probability

### Assignment

The next 2 questions refer to the following scenario. Suppose the manager of a pet store wants to determine if there is a difference in the amount of money spent in the store, on average, by owners of dogs vs. owners of cats. Consider dog owners as group 1 and cat owners as group 2. Assume that the population standard deviations are equivalent between groups. Below are the sample data for the nine dog owners and the 9 cat owners. Test the hypothesis at alpha equals 1%.

The hypothesis at  $H_0: \mu_1 = \mu_2$  vs.  $H_a: \mu_1 \neq \mu_2$ .

Group1	Group 2
36	35.5
19	32.5
24.5	30
27	31.5
20	35.5
35	38
24.5	34.5
23.5	36
27.5	26

15) What is the p-value and test statistic used to test this hypothesis?

- a) 0.0162 2.134
- b) 0.9961 -2.134
- c) 0.0339 3.044
- d) 0.0756 3.044
- e) 0.0077 -3.044

16) Is there a significant difference in the amount of money spent in the pet store, on average, by owners of dogs vs. c

### Solution

Assumptions: 1. Both populations are normal. 2. The population standard deviations  $\sigma_1$  and  $\sigma_2$  are equal. From Excel data analysis (t-test: two sample assuming equal variances) we obtain p-value=0.0086 (two-tail), t-stat=-2.99, t critical two-tail=2.92. Since the p-value is 0.0086 is less than significance level 0.01, it can be concluded that there is a difference between means, so the evidence of  $H_a$  is moderately strong.

Now we apply statistical methods. The hypothesis at  $H_0: \mu_1 = \mu_2$  vs.  $H_a: \mu_1 \neq \mu_2$ . Let  $X_i$  be observations from Group 1,  $i = 1, \dots, 9$ , let  $Y_j$  be observations from Group 2. Calculate  $n_1 = n_2 = 9$ , sample means  $\bar{X} = 26.33$ ;  $\bar{Y} = 33.28$ , sample standard deviations  $s_1^2 = 5.91$ ,  $s_2^2 = 3.68$ .

$$s_{pooled}^2 = \frac{(n_1-1)s_1^2 + (n_2-1)s_2^2}{n_1+n_2-2} = \frac{8*5.91+8*3.68}{16} = 4.79$$

We employ test statistic

$$T = \frac{\bar{X} - \bar{Y}}{s_{pooled} \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}} = \frac{(26.33 - 33.28)}{\sqrt{4.79} * \frac{\sqrt{2}}{3}} * 4.79 = -32.41, \text{d.f.} = n_1 + n_2 - 2 = 16, \text{we approximate the}$$

tabled value as  $t_{0.01} = 2.92$ , so the rejection region is  $R: |T| \geq t$ . It is true, this value lies in the rejection region  $R$ . Consequently, at the 0.01 level of significance, we reject the null hypothesis in favour of the alternative hypothesis that there is a significant difference in the amount of money spent in the pet store, on average, by owners of dogs vs. c