

Answer on Question#37766 – Math – Combinatorics

How many 4 digit numbers are there where repetition of digits are allowed?

Solution

By fundamental principle of Counting, if one thing can be accomplished n_1 different ways and after this a second thing can be accomplished n_2 different ways, ... , and finally a k th thing can be accomplished in n_k different ways, then all k things can be accomplished in the specified order in $n_1 * n_2 * \dots * n_k$ different ways.

In real numbers the first digit can be any of 1,2,3,4,5,6,7,8,9, so, the first digit can be chosen 9 different ways. The second digit, the third and the fourth ones are any, including 0 (each of them can be chosen 10 different ways). Therefore, in case where repetition of digits are allowed, there are $9 * 10 * 10 * 10 = 9000$ 4-digit numbers.

In case of sequences of symbols, not numbers, there are $10 * 10 * 10 * 10 = 10000$ 4-digit sequences of digits.