

$$f(x) = 2x(x+1)^2$$

1. Domain: $x \in \mathbb{R}$

2. Range: $y \in \mathbb{R}$

3. $f(-x) = -2x(-x+1)^2$, hence function is not even nor odd.

4. $\lim_{x \rightarrow -\infty} f(x) = \infty$, $\lim_{x \rightarrow \infty} f(x) = -\infty$.

5. $f'(x) = 2(x+1)^2 + 4x(x+1) = 0$, which has solutions $x = -1$ and $x = \frac{-1}{3}$. The signs of $f'(x)$ are as follows: $++$ for $(-\infty; -1)$, $(-1; -\frac{1}{3})$, $(\frac{-1}{3}; \infty)$ respectively, hence function is increasing,

decreasing and increasing again on corresponding intervals. $x = -1$ is local maximum and $x = \frac{-1}{3}$ is local minimum.

6. $f''(x) = 4x + 8(1+x) = 0$, which has solutions $x = \frac{-2}{3}$ - this is the inflection point. For $x \in (-\infty, -\frac{2}{3})$, function is concave down and for $x \in (-\frac{2}{3}, \infty)$ it is concave upward.

7. There are no horizontal and vertical asymptotes. Also there are no slant asymptotes.

