

Answer on question 35641 – Math – Calculus

Compute the surface area generated by revolving the curve $f(x)=2\sqrt{x}$, $1 \leq x \leq 4$ about the x axis.

Solution

We will use the formula

$$S = 2\pi \int_a^b f(x) \sqrt{1 + (f'(x))^2} dx$$

to find the surface area .

So we have

$$S = 2\pi \int_1^4 2\sqrt{x} \sqrt{1 + \left(\frac{1}{\sqrt{x}}\right)^2} dx = 4\pi \int_1^4 \sqrt{x+1} dx = 4\pi * \frac{2}{3} (x+1)^{\frac{3}{2}} \Big|_1^4 = \frac{8\pi}{3} (5\sqrt{5} - 2\sqrt{2}).$$

Answer: $\frac{8\pi}{3} (5\sqrt{5} - 2\sqrt{2})$.