

**a)**

By definition, normal cone for a set  $X$  at point  $x$  is defined in such a way:

$$N_X(x) = \{z | \exists x_k \in X, \{z_k\} \text{ s. t. } z_k \in T_X(x_k)^*, x_k \rightarrow x, z_k \rightarrow z\}$$

Here  $T_X(x)$  is the tangent cone to the set  $X$  at point  $x$ . It is defined in such a way:

$$T_X(x) = \{0\} \cup \left\{ y \mid y \neq 0, \exists \{x_k\} \subset X \text{ s. t. } x_k \neq x \text{ and } x_k \rightarrow x, \frac{x_k - x}{\|x_k - x\|} \rightarrow \frac{y_k}{\|y\|} \right\}$$

Without losing generality, let  $x$  be a point at the origin and circular region  $C$  lies in the upper half-plane. Since the tangent cone equals to

$T_X(x) = \{(x, y) | y > 0\}$  the normal cone equals to

$$N_X(x) = \{(x, y) | y = 0\}$$

**(b)**

In case  $C$  is rectangular region in  $R^2$ ,  $x$  is point on the boundary, then as in (a)

$$T_X(x) = \{(x, y) | y > 0\}$$

$$N_X(x) = \{(x, y) | y = 0\}$$