

Consider expansion of  $(x + y)^n$ :

$$(x + y)^n = \sum_{i=0}^n \binom{n}{i} x^i y^{n-i}$$

We need to find coefficient at term  $x^3 y^3$ .

We see that all terms of the expansion are in form  $x^k y^{n-k}$ . So if  $n \neq 6$  coefficient at  $x^3 y^3$  equals to 0.

If  $n = 6$  the coefficient at  $x^3 y^3$  equals to

$$\binom{6}{3} = \frac{6 \cdot 5 \cdot 4}{3!} = 20$$