

Answer on Question # 34605 – Math – Trigonometry

Question: Which pair represents $(4, -4)$ in polar plane?

- A. $(6.56, 47.77)$
- B. $(6.56, 43.77)$
- C. $(5.66, 44.76)$**
- D. $(5.56, 47.77)$

Solution

We use the following formulas:

$$x = r \cos \varphi$$

$$y = r \sin \varphi$$

where (x, y) is defined in Cartesian coordinate system.

So, we have the system:

$$\begin{cases} 4 = r \cos \varphi \\ -4 = r \sin \varphi \end{cases} \text{. Divide the second by the first one:}$$

$$\tan \varphi = -1 \Rightarrow \varphi = \frac{1}{4}(4\pi n - \pi), n \in \mathbb{Z}.$$

$$\text{So } r = \frac{4}{\cos \frac{\pi}{4}} = 4\sqrt{2} \approx 5.66$$

Answer: C. $(5.66, 44.76)$