

$$f(x) = 2x + 6$$

Dividing interval  $[0, 3]$  into  $n$  equal subintervals we will get such set of intervals:

$$\left\{ \left[ \frac{3i}{n}, \frac{3(i+1)}{n} \right], i = 0, \dots, n-1 \right\}$$

Since  $f(x)$  is monotonic the upper sum equals to

$$\begin{aligned} S_n &= \frac{3}{n} \sum_{i=0}^{n-1} f\left(\frac{3(i+1)}{n}\right) = \frac{3}{n} \sum_{i=0}^{n-1} \left( 2\left(\frac{3(i+1)}{n}\right) + 6 \right) \\ &= \frac{3}{n} \left( \frac{6}{n} \sum_{i=0}^{n-1} i + n \cdot \left(\frac{6}{n} + 6\right) \right) = \frac{3}{n} \left( \frac{6(n-1)n}{2} + 6 + 6n \right) \\ &= \frac{9(n-1)}{n} + \frac{18}{n} + 18 \end{aligned}$$

Taking limit as  $n$  approaches to infinity we get:

$$\lim_{n \rightarrow \infty} \frac{9(n-1)}{n} + \frac{18}{n} + 18 = 9 + 18 = 27$$

So the area under the curve  $f(x)$  over  $[0, 3]$  equals 27.