

Find the integral of $x \cos ax^2 dx$ with respect to x

- a. $\cos^3 x + c$
- b. $\sin^2 x + c$
- c. $\sec^2 x + 1$
- d. $\frac{1}{2a} \sin ax^2 + c$

Solution.

Let's integrate it:

$$\int x \cos ax^2 dx$$

Substitute $ax^2 = t$, then $dt = 2ax dx$. We have

$$\int x \cos ax^2 dx = \int \frac{1}{a2} \cos ax^2 \cdot 2ax dx = \frac{1}{2a} \int \cos t dt = \frac{1}{2a} \sin t + c$$

Substitute back $t = ax^2$:

$$\frac{1}{2a} \sin t + c = \frac{1}{2a} \sin ax^2 + c$$

Answer:

- d. $\frac{1}{2a} \sin ax^2 + c$.