32980:

Task.

Let

T:U→V

be a linear transformation, where U and V are of the same finite dimension. Then the following but one statements are equivalent

T is a homomorphism

T is an isomorphism

T is 1 - 1

T is onto

## Solution.

Isomorphism is a one-to-one relation onto the map between two sets, which preserves the relations existing between elements in its domain. Let  $T:U \rightarrow V$  be a linear transformation, where U and V are of the same finite dimension. Then T is an isomorphism. Thus, the statement "T is a homomorphism" is not true.

Answer. "T is a homomorphism" is the only non-equivalent statement.