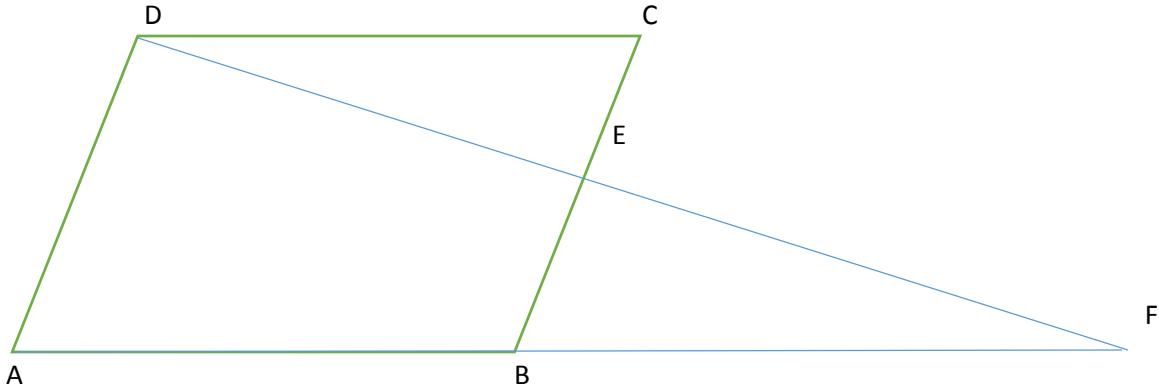


Answer on Question # 32644 – Math – Geometry

ABCD is a parallelogram and E is the midpoint of BC. DE and AB are produced to meet at F. Show that $AF=2AB$.

Solution.



If we prove that triangles DEC and BFE are equal we show that $AF=2AB$.

So,

- 1) As E is the midpoint of BC we have that $BE=EC$;
- 2) $\text{Angle}(DEC)=\text{angle}(BEF)$, as vertical angles;
- 3) $\text{Angle}(C)=\text{angle}(EBF)$, as in parallelogram $\text{angle}(A)=\text{angle}(C)$ and $\text{angle}(180-A)=\text{angle}(B)$.

From 1)-3) we make a conclusion that $\text{triangle}(DEC)=\text{triangle}(BFE)$. And $BF=DC$. As ABCD is a parallelogram we obtain that $BF=AB$.

Thus, $AF=2AB$.