

Task. A tap can fill a tank in 15 minutes and another tap attached to the same tank when opened can empty it in 8 minutes. If both taps are opened at the same time, the tank will be empty in WHAT minutes? or filled in WHAT minutes?

Solution. Let X be the volume of the tank. Then the first tap can fill the tank in 15 minutes, so each minute the volume in tank will be increased by $\frac{X}{15}$.

On the other hand, the second tap can empty the tank in 8 minutes, so each minute the volume in tank will be decreased by $\frac{X}{8}$.

Therefore when both taps are opened, then each minute the volume in the tank will be changed by

$$\frac{X}{15} - \frac{X}{8} = \frac{(8 - 15)X}{15 * 8} = -\frac{7}{120} X.$$

Thus the volume will be decreased and tank will be empty.

Now suppose that tank was full and we opened both taps. Then it will be empty in

$$\frac{X}{\frac{7}{120} X} = \frac{120}{7} \text{ min.} = \frac{120 * 60}{7} \text{ sec.} \approx 1027 \text{ sec} = 17 * 60 + 8 = 17 \text{ min } 8 \text{ sec.}$$

Answer. The tank will be empty in 17 minutes and 8 seconds.