

There are 5044 brownies and cupcakes all together. The number of brownies is \$448 more than the cupcakes. After  $\frac{4}{5}$  of the brownies and  $\frac{1}{4}$  of the cupcakes was sold, the number of brownies is two times of the cupcakes. Each brownie is 80 cents less than the cupcake. How much does each brownie cost?

Solution: We assume, that price of one brownie is  $x$  dollars. Then, price of one cupcake is  $(x + 0.8)$  dollars. Let the initial number of brownies be  $y$ . Then, initial number of cupcakes is  $(5044 - y)$ .

If the initial number of brownies is \$448 more than the cupcakes, it means that difference between total initial cost of  $y$  brownies and total cost of  $(5044 - y)$  cupcakes is \$448. The respective equation is:

$$y \cdot x - (5044 - y) \cdot (x + 0.8) = 448.$$

After  $\frac{4}{5}$  of the brownies was sold, there remains a  $\frac{1}{5}$  of the initial number of brownies, it is  $y/5$ .

After  $\frac{1}{4}$  of the cupcakes was sold, there remains a  $\frac{3}{4}$  of the initial number of cupcakes, it will be  $(5044 - y) \cdot \frac{3}{4}$ . According to the condition of the task, the number of remained brownies is two times bigger than the number of remained cupcakes. We can write it as an equation:

$$y/5 = 2 \cdot (5044 - y) \cdot 3/4.$$

Thus, we obtained a system of 2 equations with 2 variables –  $x$  and  $y$ . After simplifying it will look as:

$$\begin{cases} 2x \cdot y - 5044x + 0.8y = 4483.2 \\ \frac{2}{15}y = 5044 - y \end{cases} \Rightarrow \begin{cases} 2x \cdot 4450.6 - 5044x + 0.8 \cdot 4450.6 = 4483.2 \\ y = 4450.6 \end{cases} \Rightarrow 3857.2x = 922.7$$

Then,  $x = 0.24$  dollars = 24 cents.

Answer: 24 cents.