Conditions

if $(1+x+x^2) = a0 + a1x + a2x^2 + ... + a2nx^2n$, then a0 + a3 + a6 + ... =? [a2 means a subscript 2 & so on...]

Solution

$$1+x+x^2=a_0+a_1x+a_2x^2+\cdots+a_{2n}x^{2n}$$

As we may see, in the left hand we have all coefficients equal to 0, except first three, whose are equal to 1. Hence,

$$a_0 = 1$$

$$a_3 = 0$$

$$a_6 = 0$$

And
$$a_0 + a_3 + a_6 = 1$$

Answer: 1