

A hundred squash balls are tested by dropping from a height of 100 inches and measuring the height of the bounce. A ball is “fast” if it rises above 32 inches. The average height of bounce was 30 inches and the standard deviation was $\frac{3}{4}$ inches. What is the chance of getting a “fast” standard ball?

We have normal distribution with mean 30 inches and standard deviation $\frac{3}{4}$:

$$m = 30$$

$$\sigma = \frac{3}{4}$$

And we need to know:

$$P(x > 32)$$

$$P(x > 32) = \int_{32}^{\infty} f(x) dx$$

$f(x)$ - probability density function

The normal distribution has probability density:

$$f(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-m)^2}{2\sigma^2}}$$

Therefore:

$$P(x > 32) = \int_{32}^{\infty} \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-m)^2}{2\sigma^2}} dx$$

Calculating this integral:

$$P(x > 32) = 0.00383 = 0.383 \%$$

Answer: 0.383 %