

Task:

at a recent concert, the 1,000-seat hall was full. Tickets bought in advance cost \$30, and tickets at the door cost \$40. Total ticket sales were 38,000. Write a system of two equations to represent this information

Solution:

Lets customers bought in advance x tickets and bought at the door y tickets. Amount of tickets sold is $x + y = 1000$ and the total cost of tickets sold is $30x + 40y = 38000$. So we have system of equations:

$$\begin{cases} x + y = 1000 \\ 30x + 40y = 38000 \end{cases}$$

Solve it: $\begin{cases} x + y = 1000 \\ 30x + 40y = 38000 \end{cases} \begin{cases} x = 1000 - y \\ 30(1000 - y) + 40y = 38000 \end{cases}$

$$\begin{cases} x = 1000 - y \\ 30000 - 30y + 40y = 38000 \end{cases} \begin{cases} x = 1000 - y \\ 30000 + 10y = 38000 \end{cases} \begin{cases} x = 1000 - y \\ 30000 + 10y = 38000 \end{cases}$$
$$\begin{cases} x = 1000 - y \\ 10y = 38000 - 30000 \end{cases} \begin{cases} x = 1000 - y \\ 10y = 8000 \end{cases} \begin{cases} x = 1000 - y \\ y = 800 \end{cases} \begin{cases} x = 1000 - 800 \\ y = 800 \end{cases} \begin{cases} x = 200 \\ y = 800 \end{cases}$$

Answer: 200 tickets bought in advance, 800 tickets bought at the door.