

Question #27826

Express this complex number in trigonometric form $(5/2)\sqrt{3} + (5/2)i$.

Solution. A complex number z is in trigonometric form if $z = r(\cos\varphi + i\sin\varphi)$, where $r = |z|$.

Denote $z = \frac{5}{2}\sqrt{3} + \frac{5}{2}i$. Then $z = 5\left(\frac{\sqrt{3}}{2} + \frac{1}{2}i\right)$. It follows immediately that $\cos\varphi = \frac{\sqrt{3}}{2}$, $\sin\varphi = \frac{1}{2}$ and $r = 5$ and so $\varphi = \frac{\pi}{6}$. Thus, $z = 5\left(\cos\frac{\pi}{6} + i\sin\frac{\pi}{6}\right)$.

Answer. $5\left(\cos\frac{\pi}{6} + i\sin\frac{\pi}{6}\right)$.