

solve the logarithmic equation:

$$x = (\log_2 \sqrt{2})^3$$

Solution:

- 1) $\sqrt{2} = 2^{\frac{1}{2}} \Rightarrow (\log_2 \sqrt{2})^3 = (\log_2 2^{\frac{1}{2}})^3$
- 2) Delivers the power of two of the logarithm in accordance with the property of the logarithm $\Rightarrow (\log_2 2^{\frac{1}{2}})^3 = (\frac{1}{2} \log_2 2)^3$
- 3) $\log_2 2 = 1 \Rightarrow (\frac{1}{2} \log_2 2)^3 = (\frac{1}{2} * 1)^3$
- 4) We raise this expression to the cube and get $(\frac{1}{2} * 1)^3 = \frac{1}{8}$

$$x = (\log_2 \sqrt{2})^3 = (\log_2 2^{\frac{1}{2}})^3 = (\frac{1}{2} \log_2 2)^3 = \frac{1}{8}$$

Answer: $x=1/8$