

### Question #27505

1. Determine the derivative of the following functions, and simplify.

a)  $f(x) = 2x^2(3x^3 - 4)$

b)  $y = 1/(5x-1)^3$

c)  $g(x) = (2x^2 - 3)^{1/3}$

**Solution.**

a)  $f(x) = 2x^2(3x^3 - 4) = 6x^5 - 8x^2.$

$$f'(x) = 30x^4 - 16x.$$

b)  $y = \frac{1}{(5x-1)^3}.$

$$y' = \frac{-3 \cdot 5}{(5x-1)^4} = -\frac{15}{(5x-1)^4}.$$

c)  $g(x) = (2x^2 - 3)^{\frac{1}{3}}.$

$$g'(x) = \frac{1}{3}(2x^2 - 3)^{-\frac{2}{3}} \cdot 4x = \frac{4x}{3^3 \sqrt{(2x^2 - 3)^2}}.$$

**Answer.**  $f'(x) = 30x^4 - 16x$ ,  $y' = \frac{-15}{(5x-1)^4}$ ,  $g'(x) = \frac{4x}{3^3 \sqrt{(2x^2-3)^2}}.$