

The current population of a town is 10,000. If the population,  $P$ , increases by 20% each year, which equation could be used to find the population after  $t$  years?

**Solution:**

For answer to this question we need to use the compound interest formula

$$P = P_0(1 + i)^n$$

Where  $P_0$ -start population,  $i$ -is the effective interest rate per period, and  $n$ -represents the number of periods.

In our task  $P_0 = 10,000$ ,  $i = 0.2$  and  $n = t$ .

At last we have:

$$P(t) = 10,000 * (1.2)^t$$

**Answer:**  $P(t) = 10,000 * (1.2)^t$

**Remark**

In real it is all well-known formula. You can read about Compound interest in WIKI [http://en.wikipedia.org/wiki/Compound\\_interest](http://en.wikipedia.org/wiki/Compound_interest)

If you need a mathematical proof let's look at the interest for a couple of years

To find a formula for future value, we'll write  $PV$  for your starting principal, and  $r$  for the rate of return expressed as a decimal. (So if the interest rate is 10%,  $r$  equals 0.1).

Your balance will grow according to the following

Now  $PV$

First year  $PV + r * PV$

Second year  $(PV + r * PV) + r * (P + r * PV)$

This starts to get messy in a hurry. But you can simplify it by noticing that you can keep pulling out factors of  $(1 + r)$  from each line. If you do that, the balances collapse to a simple pattern:

Now  $P$

First year  $PV + r * PV = PV * (1 + r)$

Second year  $(PV + r * PV) + r * (PV + r * PV) = (PV + r * PV)(1 + r) = PV(1 + r)(1 + r) = PV(1 + r)^2$

And so on.

If you follow this pattern out for  $Y$  years, you get the general formula for future value:

$$FV = PV * (1 + r)^t$$

