

The current population of a town is 10,000. If the population, P, increases by 20% each year, which equation could be used to find the population after t years?

Solution:

For answer to this question we need to use the compound interest formula

$$P = P_0(1 + i)^n$$

Where P_0 -start population, i -is the effective interest rate per period, and n -represents the number of periods.

In our task $P_0 = 10,000$, $i = 0.2$ and $n = t$.

At last we have:

$$P(t) = 10,000 * (1.2)^t$$

Answer: $P(t) = 10,000 * (1.2)^t$

Remark

In real it is all well-known formula. You can read about Compound interest in WIKI
http://en.wikipedia.org/wiki/Compound_interest

If you need a mathematical proof let's look at the interest for a couple of years

To find a formula for future value, we'll write PV for your starting principal, and r for the rate of return expressed as a decimal. (So if the interest rate is 10%, r equals 0.1).

Your balance will grow according to the following

Now

$$PV$$

First year

$$PV + r * PV$$

Second year

$$(PV + r * PV) + r * (PV + r * PV)$$

This starts to get messy in a hurry. But you can simplify it by noticing that you can keep pulling out factors of $(1 + r)$ from each line. If you do that, the balances collapse to a simple pattern:

Now

$$P$$

First year

$$PV + r * PV = PV * (1 + r)$$

Second year

$$(PV + r * PV) + r * (PV + r * PV) = (PV + r * PV)(1 + r) = PV(1 + r)(1 + r) = PV(1 + r)^2$$

And so on.

If you follow this pattern out for Y years, you get the general formula for future value:

$$FV = PV * (1 + r)^t$$

