

$$\int \frac{y+4}{y+16} dy$$

Solution:

$$\begin{aligned} \int \frac{y+4}{y+16} dy &= \int \frac{y+16-12}{y+16} dy = \int \left(\frac{y+16}{y+16} - \frac{12}{y+16} \right) dy = \\ &= \int \left(1 - \frac{12}{y+16} \right) dy = \int dy - 12 \int \frac{dy}{y+16} = y - 12 \int \frac{d(y+16)}{y+16} = \\ &= y - 12 \ln|y+16| + C = y - \ln(y+16)^{12} + C. \end{aligned}$$

Answer:

$$y - \ln(y+16)^{12} + C$$