

I want to evaluate the limit as x goes to 2 for $((\sqrt{6-x})-2)$ divided by $((\sqrt{3-x})-1)$. I would really appreciate it.

$$\lim_{x \rightarrow 2} \frac{\sqrt{6-x} - 2}{\sqrt{3-x} - 1}$$

Multiply the numerator and denominator by $(\sqrt{6-x} + 2)(\sqrt{3-x} + 1)$

$$\lim_{x \rightarrow 2} \frac{(\sqrt{6-x} - 2)(\sqrt{6-x} + 2)(\sqrt{3-x} + 1)}{(\sqrt{3-x} - 1)(\sqrt{6-x} + 2)(\sqrt{3-x} + 1)} = \lim_{x \rightarrow 2} \frac{(6-x-4)(\sqrt{3-x} + 1)}{(3-x-1)(\sqrt{6-x} + 2)} =$$

$$\lim_{x \rightarrow 2} \frac{(-x+2)(\sqrt{3-x} + 1)}{(-x+2)(\sqrt{6-x} + 2)} = \lim_{x \rightarrow 2} \frac{(\sqrt{3-x} + 1)}{(\sqrt{6-x} + 2)} = \frac{1+1}{2+2} = \frac{1}{2}$$