

The atmospheric pressure P in pounds per square inch (psi) is given by

$$P = 14.7 e^{-0.21a}$$

where a is the altitude above sea level (in miles). If a city has an atmospheric pressure of 13.35 psi, what is its altitude? (Recall that 1 mi = 5,280 ft. Round your answer to the nearest foot.)

Solution:

$$P = 14.7 e^{-0.21a}, \text{ where } a \text{ is the altitude above sea level (in miles).}$$

Given $P = 13.35$, so

$$13.35 = 14.7 e^{-0.21a}$$

Dividing both sides on 14.7 obtain

$$e^{-0.21a} = \frac{13.35}{14.7}$$

Using definition of a logarithm

$y = \ln x$ means that $x = e^y$, so

$$-0.21a = \ln \frac{13.35}{14.7} = -0.09633$$

$$a = \frac{-0.09633}{-0.21} = 0.4587 \text{ mi}$$

1 mi = 5,280 ft, so

$$a = 0.4587 \times 5,280 = 2,422 \text{ ft}$$

Answer: 2,422 ft