

**Question 1.** Simplify the expression:  $[(A \cup B)' \Delta B] \cup B'$

*Solution.* We have

$$\begin{aligned} [(A \cup B)' \Delta B] \cup B' &= [((A \cup B)' \cap B') \cup ((A \cup B)'' \cap B)] \cup B' \\ &= [(A' \cap B' \cap B') \cup ((A \cup B) \cap B)] \cup B' \\ &= [(A' \cap B') \cup B] \cup B' \\ &= (A' \cap B') \cup (B \cup B') \\ &= (A' \cap B') \cup U \\ &= U, \end{aligned}$$

where  $U$  denotes the universe which contains  $A$  and  $B$ .

*Answer:* the universe  $U$ . □