

We know that the irreducible characters $\{\chi_i\}$ form an orthonormal basis for $Fk(G)$ under $[\ , \]$. If $f = \sum_i a_i \chi_i$, we see immediately that $[f, \chi_j] = [\sum_i a_i \chi_i, \chi_j] = a_j$.