Let G,G' be abelian groups of order n, and let $k = \mathbb{C}$. Since k has no proper algebraic extensions, Wedderburn's Theorem implies that kG, kG' are both isomorphic (as k-algebras) to $k \times \cdots \times k$ (n factors). But of course, G and G' need not be isomorphic!