

Conditions

Suppose $f(x)=(8-5x)e^x$

(critical number: $3/5$)

B) use interval notation to find where $f(x)$ is increasing and decreasing

C) Use interval notation where $f(x)$ is concave up and concave down

D) List values of inflection

Solution

Let's analyze the intervals of increasing and decreasing:

$$f'(x) = 8e^x - 5e^x - 5xe^x = e^x(3 - 5x)$$

We can really see, that the critical number is $3/5$.

From the left side of this point, the derivative is positive, so our function is increasing there.

From the right side – the opposite situation.

We can make a conclusion, that $f(x)$ increasing at:

$$x \in \left(-\infty, \frac{3}{5}\right)$$

Decreasing at:

$$x \in \left(\frac{3}{5}, \infty\right)$$

The information about where is our function concave up or down can give us the 2nd derivative:

$$f''(x) = 3e^x - 5e^x - 5xe^x = -e^x(2 + 5x)$$

The critical value is $-2/5$. From the right side of this value, the derivative is negative, so the function is concave up. From the left side – the opposite situation.

We can make a conclusion, that $f(x)$ concave up at:

$$x \in \left(-\frac{2}{5}, \infty\right)$$

Concave down at:

$$x \in \left(-\infty, -\frac{2}{5}\right)$$

The only value of inflection is the point $-2/5$